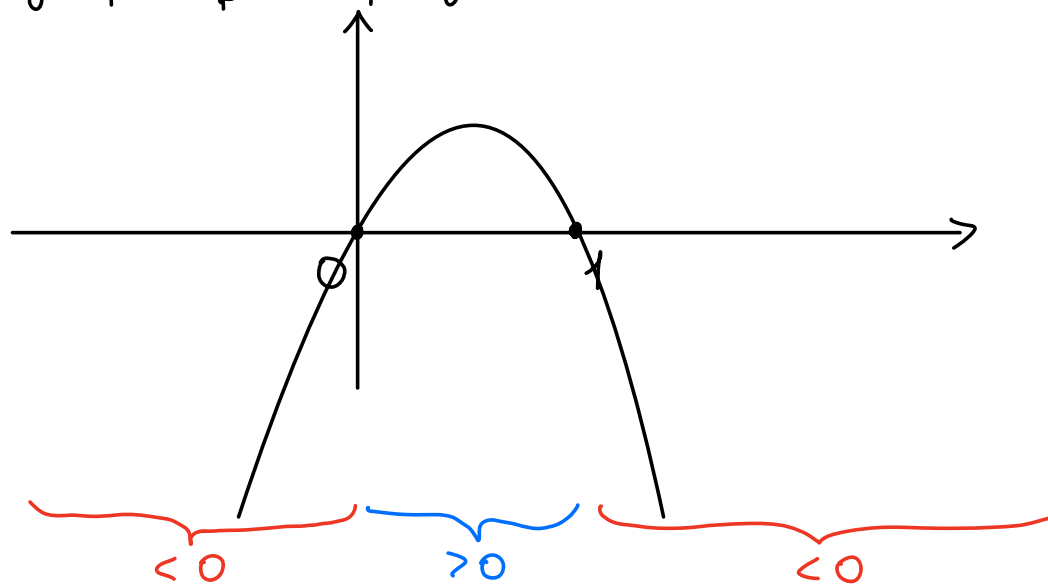


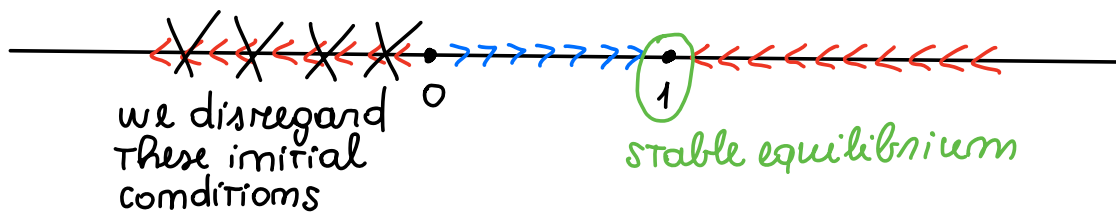
LOGISTIC EQUATION: PHASE LINE

$$y'(\tau) = y(\tau)(1 - y(\tau))$$

The graph of the polynomial $y(1-y)$ is



Hence the phase line is given by

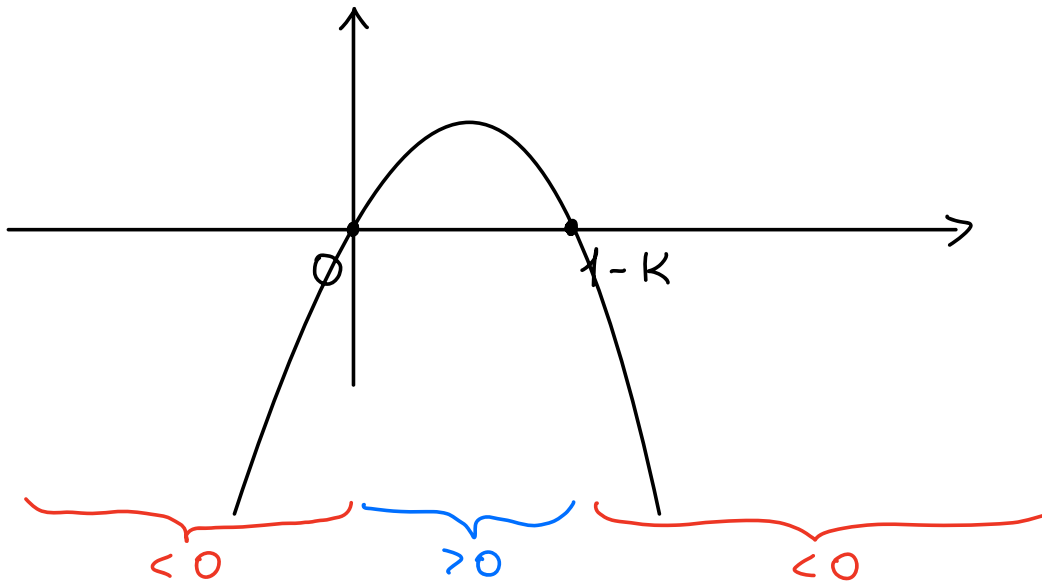


LOGISTIC EQUATION WITH PROPORTIONAL HARVESTING: PHASE LINE

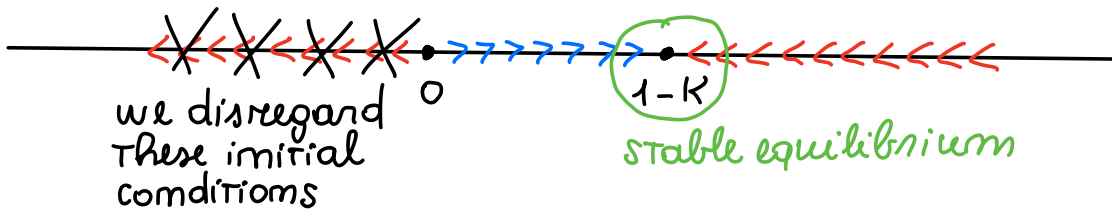
$$y'(\tau) = y(\tau)(1 - y(\tau)) - Ky(\tau)$$

• Case $K < 1$

The graph of the polynomial $y(1 - K - y)$ is

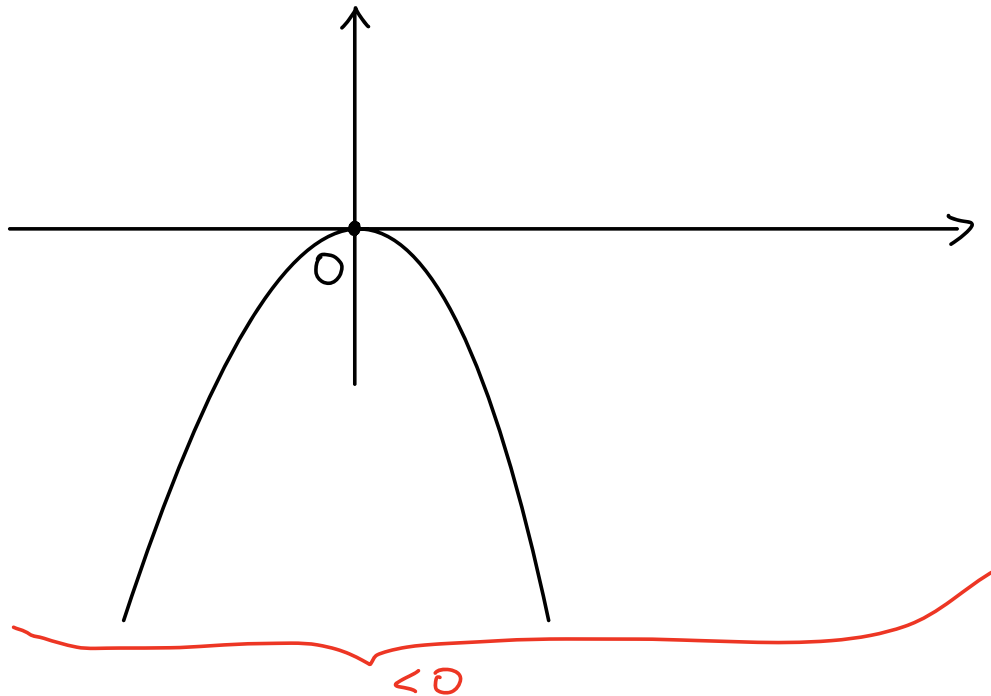


Hence the phase line is given by

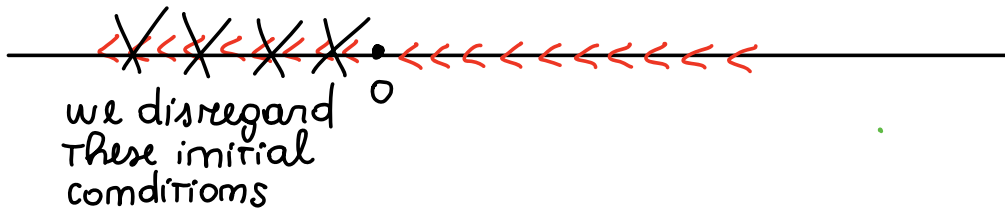


• Case $K=1$

The graph of The polynomial $-y^2$ is

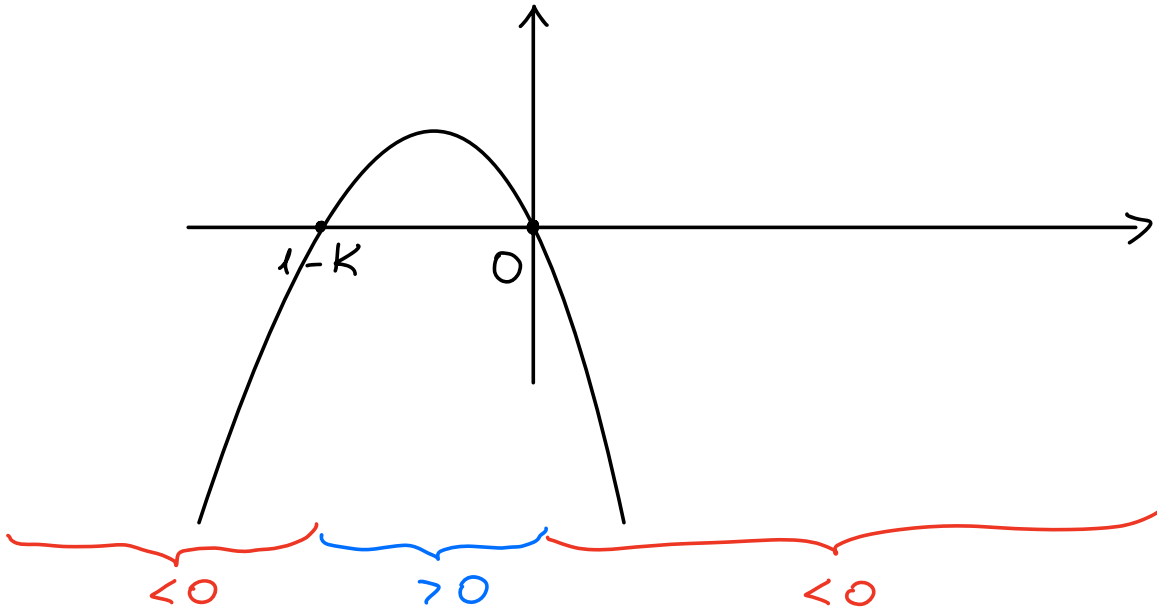


Hence The phase line is given by



• Case $K > 1$

The graph of the polynomial $Y(1 - K - Y)$ is



Hence the phase line is given by

